# The Number of Undocumented Immigrants in the United States: Estimates Based on Demographic Modeling with Data from 1990 to 2016 

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#### Abstract

We apply standard demographic principles of inflows and outflows to estimate the number of undocumented immigrants in the United States, using the best available data, including some that have only recently become available. Our analysis covers the years 1990 to 2016. We develop an estimate of the number of undocumented immigrants based on parameter values that tend to underestimate undocumented immigrant inflows and overstate outflows; we also show the probability distribution for the number of undocumented immigrants based on simulating our model over parameter value ranges. Our conservative estimate is 16.7 million for 2016 , nearly fifty percent higher than the most prominent current estimate of 11.3 million, which is based on survey data and thus different sources and methods. The mean estimate based on our simulation analysis is 22.1 million, essentially double the current widely accepted estimate. Our model predicts a similar trajectory of growth in the number of undocumented immigrants over the years of our analysis, but at a higher level. While our analysis delivers different results, we note that it is based on many assumptions. The most critical of these concern border apprehension rates and voluntary emigration rates of undocumented immigrants in the U.S. These rates are uncertain, especially in the 1990's and early 2000's, which is when - both based on our modeling and the very different survey data approach - the number of undocumented immigrants increases most significantly. Our results, while based on a number of assumptions and uncertainties, could help frame debates about policies whose consequences depend on the number of undocumented immigrants in the United States.


## Introduction

Immigration policy remains a hotly debated issue in the United States, with perhaps no aspect more controversial than how to address undocumented immigrants who do not have legal status. Policy debates about the amount of resources to devote to this issue,
and the merits of alternative policies, including deportation, amnesty, and border control, depend critically on estimates of the number of undocumented immigrants in the U.S., which sets the scale of the issue. The most widely accepted estimate of this number currently is approximately 11.3 million $(1,2)$. This estimate is based on variants of the residual method (2-4). In this method, the size of the unauthorized immigrant population residing in the United States is set equal to the estimate of the total foreign-born population minus the legally resident foreign-born population. The total foreign-born population estimate is derived from surveys that ask respondents whether they were born outside of the United States (and whether they are American citizens), specifically either the American Community Survey or the Current Population Survey. The legally resident foreign-born population is estimated using administrative data on legal admissions.

An alternative approach to estimating the size of the undocumented population follows directly from basic demographic principles. Starting from a known population size at a given date, the population size at a future date equals the starting value plus the cumulative inflows minus the cumulative outflows. We employ this approach to estimate the number of undocumented immigrants in the U.S. for each year from 1990 to 2016 , using the best available data and parameter values from the academic literature and government sources. Some of the information we use has been collected and made available only recently, so our approach is timely.

Our analysis has two main outputs. First, we generate what we call our conservative estimate, using parameter values that intentionally underestimate population inflows and overestimate population outflows, leading to estimates that will tend to underestimate the number of undocumented immigrants. Our conservative estimate for 2016 is 16.7 million, well above the estimate that is most widely accepted at present, which is for 2015 but should be comparable ${ }^{1}$ For our second step, recognizing that there is significant uncertainty about population flows, we simulate our model over a wide range of values for key parameters. These parameter values range from very conservative estimates to standard values in the literature. We sample values for each key parameter from uniform distributions over the ranges we establish. In our simulations, we also include Poisson population uncertainty conditional on parameter values, thus addressing the inherent variability in population flows. Our simulation results produce probability distributions over the number of undocumented immigrants for each year from 1990 to 2016. The results demonstrate that our conservative estimate falls towards the bottom of the probability distribution, at approximately the 2.5 th percentile. The mean of the 2016 distribution is 22.1 million, which we take as the best overall estimate of the number of undocumented immigrants based on our modeling approach and current data. We also show the variability in our model based on the simulations for each year from 1990 through 2016.

## Methods

[^0]simulations we assume that the starting population is drawn from a Poisson distribution with a mean of 3.5 million. It then follows that the population size at a future date equals the starting value plus the cumulative inflows minus the cumulative outflows.

## Population Inflows

Population inflows are decomposed into two streams: (I) undocumented immigrants who initially entered the country legally but have overstayed their visas; and (II) immigrants who have illegally crossed the border without being apprehended. We describe our approach for each source, explain the basis for our assumptions and why they are conservative, and list parameter ranges for the simulation.
(I) Visa overstays are estimated using Department of Homeland Security (DHS) data for 2016, the first year for which visa overstays were comprehensively measured (5). To apply this data in our context we also gather data for non-immigrant visas issued for all years from 1990 (6). For our conservative estimate we assume that for each year the rate of overstays was equal to the 2016 rate. Calibration of our model shows that this assumption is in fact quite conservative. In particular, approximately $41 \%$ of undocumented immigrants based on the current survey data approach are visa overstayers (7), which translates to a visa overstay population of 4.6 million in 2015. Our model however predicts the number of overstayers to be less than this (even though our overall estimate of the number of undocumented immigrants is higher).$^{3} \mathrm{We}$ compute that we would need to set the visa overstay rate above the DHS 2016 rate, specifically 1.1 times that rate, for our conservative estimate to generate as many overstayers as the 4.6 million in the 11.3 million estimate $4^{4}$ For the simulation, we set the visa overstay rate equal to the 2016 rate multiplied by a uniform draw from the range $[0.5,1.5]$; consistent with the discussion above, this is a relatively conservative range.
(II) Illegal Border Crossers: We estimate illegal border crossers through application of the standard repeated trials (capture-recapture) model $(8,9,10)$. The model requires as inputs statistics on the total number of border apprehensions, the number of individuals apprehended more than once in a year (recidivist apprehensions), and estimates of the deterrence rate - the fraction of individuals who give up after being apprehended and do not attempt another crossing. Given these inputs, the repeated trials model generates estimates of: (i) the apprehension rate - the probability an individual is caught trying to cross the border; and (ii) the total number of individuals who are not apprehended (they may be caught one or more times but cross successfully on a later attempt) and enter the interior of the country illegally - the number of illegal border crossers in a year. We discuss data sources and potential weaknesses of this approach here; more information and mathematical details are provided in the Supporting Information.

DHS $(10,11)$ provide figures for the total number of border apprehensions for every year in our timespan. They also provide information on the number of recidivist apprehensions and estimates of the deterrence rate for every year from 2005. Based on these figures and estimates they provide an estimate of the apprehension rate for each year from 2005 to 2015. Their estimate is $35 \%$ for 2005 and increases steadily, to above

[^1]$50 \%$ by the end of the sample period. From their estimates we are able to derive directly estimates of the number of illegal border crossers for each of these years. For earlier years (1990 to 2004) we must make further assumptions. Our assumptions are about the apprehension and deterrence rates, since these have been addressed in the literature; in turn we are able to generate estimates of the number of illegal border crossers in earlier years based on these assumptions (see the Supporting Information for analytic details).

Most experts agree that the apprehension rate was significantly lower in earlier years $(12,13)$. A recent study (12) using data from the Mexican Migration Project estimates this rate for every year from 1990 to 2010; estimates in the 1990's begin from the low twenties and range upwards to approximately $30 \%$. A second study estimates the rate for 2003 at around $20 \%$ (13). Given these estimates, and the general view that apprehension rates have risen, for our conservative estimate we assume that the apprehension rate in years 1990-2004 was equal to the average rate in years 2005-10 or $39 \%$; this is well above the rates discussed in the literature for earlier years and thus tends to reduce our estimate of the number of undocumented immigrants since it implies a larger fraction are apprehended at the border. For our simulation we assume a uniform distribution over the range $[0.25,0.40]$ for the earlier years, still above the average rates in the literature for these years.

Additional facts support the view that the apprehension rate has increased in recent years. The number of border agents has increased dramatically over the timespan of our analysis (14), and the number of hours spent by border agents patrolling the immediate border area has increased by more than $300 \%$ between 1992- 2004 (15). Further, new infrastructure (e.g., fences) and technologies (e.g., night vision equipment, sensors, and video imaging systems) were also introduced during this period (15). Thus the apprehension rate we use for earlier years almost certainly overstates the actual apprehension rate and therefore underestimates the number of successful crossings. 5 We note finally that in using data only on Southern Border crossings we again are conservative in our approach, not accounting for illegal crossings along other borders.

Notwithstanding our view that we make conservative choices in setting up our model and parameter values, we acknowledge that border apprehension rates for the 1990's are not based on as well-developed data sources as estimates for more recent years. Thus it remains a possibility that these rates are higher than we believe. One aspect of this uncertainty concerns deterrence. When deterrence is higher border crossings will fall. Most researchers believe deterrence has increased in recent years $(8,12)]^{6}$ One piece of evidence in support of this is data on the voluntary return rate, which refers to the percentage of individuals apprehended at the border who are released back to their home country without going through formal removal proceedings and not being subjected to further penalties. Voluntary returns are thus not "punished" and thus are less likely to be deterred from trying to cross the border in the future, compared with individuals who are subjected to stronger penalties. The voluntary return rate has fallen in recent years, from $98 \%$ between 2000 and 2004 to $84 \%$ between 2005 and 2010 . Thus, at least based on this measure deterrence efforts have increased. However, this does not conclusively demonstrate that deterrence was lower in earlier years and it remains a possibility that it was higher, which would tend to reduce our estimates of the number of undocumented immigrants. In conclusion we note that although there is much uncertainty about the border apprehension rate, it would have to be very high, above $60 \%$ for earlier years, in order to generate estimates of the 2015 population of undocumented immigrants in the range of the current widely accepted estimate of just

[^2]over 11 million ${ }^{7}$ This seems implausible based on our reading of the literature.

## Population Outflows

Population outflows are broken into four categories: (I) voluntary emigration; (II) mortality; (III) deportation; and (IV) change of status from unauthorized to lawful.
(I) Voluntary emigration rates are the largest source of outflow and the most uncertain based on limited data availability. It is well accepted that voluntary emigration rates decline sharply with time spent in the country (16); thus we employ separate emigration rates for those who have spent one year or less in the U.S., 2-10 years, or longer. We use the following values for our conservative estimate. First, for those who have spent one year or less we assume a voluntary emigration rate of $40 \%$. This estimate is based on data for the first-year visa overstay exit rate (the fraction of overstayers who left the country within one year from the day their visa expired) for 2016 (17), which is in the lower thirty percent range ${ }^{8}$ We note that the rate for visa overstayers is very likely a substantial overestimate for illegal border crossers, who are widely viewed as having a lower likelihood of exiting in the first year, especially in more recent years (12). The $40 \%$ first-year emigration rate that we assume is well above the standard values in the literature $(4,12,16,18)$, which range from $1 \%$ to $25 \%$. Hence this assumption contributes to making our estimate of the number of undocumented immigrants in the country a conservative one. For years 2-10 we assume a rate of $4 \%$ per year. This is the upper bound among estimates in the literature, which lie between 0.01 to $0.04(4,16,18))$. Lastly, for years 10 and above, published estimates of the emigration rate typically fall around $1 \%$; we set this rate to $1 \%$ per year in line with these estimates. Note that given the extremely high $40 \%$ emigration rate that we assume for those who have only been in the country for one year or less, overall annual emigration rates in our model simulation are significantly higher than those found in the literature or government sources $\frac{9}{9}$

For our simulation analysis we divide first-year voluntary emigration into two categories, visa overstayers and illegal border crossers. For visa overstayers we assume the first-year rate falls in the range [.25,.50] (uniform) for each year; based on the discussion in the preceding paragraph and literature cited there, this is a relatively conservative range with midpoint $37.5 \%$ above nearly all accepted estimates. For illegal border crossers there is data indicating that first-year voluntary emigration rates vary across cohorts (12) (we are not aware of such data for visa overstayers). To incorporate this, we assume that a voluntary emigration rate is drawn for each cohort year from a uniform distribution that is specific to that cohort's year of initial entry; the lower bound of this range is set by the numbers in (12) and the upper bound is set at 0.50 . Again our assumptions here are conservative, since we use an accepted value in the literature as our lower bound and allow emigration rates to range to very high values. For years 2-10 and 10 and above we use the same distributions for overstayers and illegal border crossers. For years $2-10$ we draw a value from the range [.01, .05], for which the mean value of $3 \%$ is relatively high and thus conservative; and for years 10 and above we draw a value from the range $[.005, .02]$, thus centered slightly above the standard value in the literature. We note that the first-year rate is the most critical for our analysis.

An important issue is circular flow of migrants, which refers to individuals who enter the country, then exit temporarily and re-enter a short time later. There is limited numerical data for circular flow rates. However, it is logical and recognized in the

[^3]literature (12) that when border apprehension rates are higher circular flow rates for border crossers tend to diminish: Given it will be more difficult to re-enter the country successfully later, illegal border crossers in the country will tend not to leave for temporary reasons. Thus this issue is important for illegal border crossers (but not likely to be as relevant for visa overstayers). Thus in our simulation we impose a negative correlation between the first-year emigration rate and the border apprehension rate for illegal border crossers; based on our own analysis for annual data from the best recent study (12) we use a correlation of -0.5 (see the Supporting Information for details). We note that this correlation does not substantially change the range or mean of our simulation results, but does reduce the variance.
(II) The mortality rate applied is the age-adjusted mortality rate reported by the Centers for Disease Control and Prevention (19). For our conservative estimate we set this value at 0.7 percent, and for the simulation we draw a value from the range [0.5,1.0] percent. We view these values as conservative. Experts in the field argue that this rate overestimates mortality among undocumented immigrants (4). To further check that our mortality rate assumptions are an overestimate and thus contribute to making our overall estimate of the number of undocumented immigrants conservative, we combined the age, gender, and country of birth distributions of undocumented immigrants reported in $(2,20)$ with CDC mortality rates $(16)$. The resulting mortality rate is much lower than the mortality rate we assume (see the Supporting Information for details). We note that the mortality rate is low relative to the voluntary emigration rate, and thus a less important parameter for the calculation we make.

Lastly, (III) the annual number of deportations is taken directly from DHS annual statistics $(11,21)$ for each year. (IV) The number of undocumented immigrants who change to legal status in each year is also taken directly from published data $(4,11)$. We include the number of deferred action for childhood arrivals (DACA) recipients as population outflows even though such individuals remain technically undocumented, which again serves to underestimate the size of the population.

## Simulation Methodology

Our simulation is designed to evaluate the range of outcomes the model produces, thus taking into account important sources of variability. There are two main sources of uncertainty: parameter uncertainty, and inherent population variability conditional upon a set of parameter values. We take both sources into account, but note that the first source is the main factor contributing to the variability of the population distribution in the model.

We address parameter uncertainty by establishing ranges for key parameters. As documented above, these key parameters are (i) the visa overstay rate; (ii) the border apprehension rate for individuals attempting to cross the border illegally; (iii) the voluntary emigration rate, which is set separately for illegal border crossers and visa overstayers for the first year and then jointly for years 2-10 and years 10 and above, and for which we establish a cohort-specific range for each annual cohort for the first-year rate for illegal border crossers; and (iv) the mortality rate. For each parameter, we establish a uniform distribution over the set range (and impose a negative correlation between the border apprehension rate and first-year voluntary emigration rate for illegal border crossers). Then, in each simulation run we sample a value for each parameter from its underlying distribution. All of the ranges for the parameter distributions have been specified in the preceding sections. We also sample a value for the initial population of undocumented immigrants in 1990 from a Poisson distribution with a mean of 3.5 million, the most widely accepted estimate of the population of
undocumented immigrants as of that date. See the Supporting Information for further details.

To model inherent population uncertainty given a set of parameter values, we impose a Poisson structure on our model. Specifically, the population in a particular year, conditional on a set of parameter values, is represented as the sum of all individuals who have entered the country in previous years and have remained in the country from their year of arrival until the particular year in question. The number of entries (in Poisson terminology, arrivals) in any year is drawn from a Poisson distribution with mean dependent upon the underlying parameter values governing apprehension probabilities and visa overstays for that year, while the probability that a new immigrant remains in the country from entry until the particular year in question is determined based on the parameters governing voluntary emigration, mortality, deportation and change-of-status rates. It follows (see the Supporting Information for mathematical details) that the number of individuals who enter the country in any given year and are still in the country at some future date will also follow a Poisson distribution. Further, the number of individuals who enter in any given year and remain in the country at a future time can be considered to be statistically independent given the underlying parameter values (see the Supporting Information for details). Thus, the population of undocumented immigrants in a particular year, which is the sum of those who have entered in past years and are still in the country in the particular year in question, also follows a Poisson distribution, for the sum of independent Poisson random variables is itself Poisson distributed.

We ran $1,000,000$ trials simulating the model. For each trial we recorded the total number of undocumented immigrants predicted to be in the U.S. in each year from 1990 through 2016 for that trial.

Following suggestions made by the Academic Editor based on comments made by a reviewer, we performed an additional set of simulations making even more conservative assumptions about net inflows over the period 1990-98. This is the period for which there is significant uncertainty about net inflows of undocumented immigrants. Specifically, we calibrated the model such that the net inflows are half a million per year over this period (in line with the residual method's estimates during this period) and computed the pooled number of undocumented immigrants at the end of 1998 based on this approach. We then simulated our model forward from that point using the same framework described above.

## Results

Figure 1 depicts our results for year 2016, the most recent year for which we are able to produce an estimate. The graph depicts the relative frequency of the number of undocumented immigrants in the U.S.; it is a smoothed version of the histogram we generate based on simulating our model $1,000,000$ times. The Figure also shows our conservative estimate of 16.7 million in Red, and the most widely accepted estimate heretofore of 11.3 million in Blue on the far left. We note that this last estimate is for 2015, but should be comparable since both the estimates based on the survey approach and our modeling approach indicate that the number of undocumented immigrants has remained relatively constant in recent years. Finally, the mean estimate of 22.1 million is shown in black in the center of the distribution. It is clear from the Figure that based on the data we use, our assumptions, and our demographic model, the currently accepted estimate falls outside the range of likely values. And our conservative estimate is indeed conservative based on our modeling approach and parameter ranges, lying at approximately the 2.5 th percentile of the probability distribution.

Figure 2 displays our simulation results for each year from 1990 through 2016. Our

Fig 1. Relative frequency probability function for the number of undocumented immigrants in the U.S.

Fig 2. The current widely accepted estimate of the number of undocumented immigrants in the U.S. (in Blue); together with our conservative estimate (in Red); and the mean value we estimate for each year (in Black).
conservative estimate of the number of undocumented immigrants for each year is shown in Red, the most widely accepted estimate (through 2015) is shown in Blue, and the mean value we estimate for each year is shown in Black. The results show that our model estimates follow a similar shaped trajectory as the widely accepted current estimates do, but grow faster and are well above those estimates for every year.

The results of our analysis are clear: The number of undocumented immigrants in the United States is estimated to be substantially larger than has been appreciated at least in widely accepted previous estimates. Even an estimate based on what we view as conservative assumptions, in some cases unrealistically so, generates an estimate of 16.7 million, well above the conventional estimate of 11.3 million. The mean of our simulations, which range over more standard but still conservative parameter values, is 22.1 million, essentially twice the current widely accepted estimate; the ninety-five percent probability interval is [16.2,29.5].

Even for the scenario presuming net inflows of 0.5 million per year for 1990-98 our results still exceed the current estimates substantially. The mean estimate is 17.0 million with a $95 \%$ probability interval of 13.5 million to 21.1 million. The conservative estimate for this scenario is 14.0 million, still significantly above the widely accepted estimate of 11.3 million.

## Discussion

It is currently fairly widely accepted that there are approximately 11 million undocumented immigrants in the United States. This estimate, derived from population surveys and legal immigration records, has formed the backdrop for the immigration policy debate in the United States. Using a different approach grounded in operational data, and demographic and mathematical modeling, we have arrived at higher estimates of the undocumented immigrant population.

A possible explanation for the discrepancy in these results is that the survey-based approach taken in (2-4) must surmount two challenges. First, it requires reaching a representative sample of all those born outside of the United States. Second, it requires accurate responses from survey respondents when asked where they were born, and whether they are American citizens. It is plausible that undocumented immigrants are more difficult to locate (and survey) than other foreign-born residents of the United States, and if contacted, undocumented immigrants might misreport their country of origin, citizenship, and/or number of household residents fearing the possible consequences of revealing their true status. Any of these circumstances would lead to underestimating the true number of undocumented immigrants.

Our approach, summarized above and detailed in the Supporting Information, is grounded in fundamental principles of demographic flows. The size of any population can be represented as its initial value plus cumulative inflows minus cumulative outflows. We have specialized this approach to the number of undocumented immigrants in the United States, and have drawn upon previously unavailable data. From border apprehensions and visa overstays, it is possible to infer the number of new undocumented arrivals by reversing the flow: how many new arrivals are necessary in

 (XLSX)
order to see the number of apprehensions and visa overstayers observed? Similarly, consideration of deportations, voluntary emigration, mortality and change-of-status enables one to infer the duration of stay in the country from the time of arrival. Together, this logic enables reconstructing the arrival and departure processes governing population inflows and outflows that result in the population of undocumented immigrants in the country.

In developing estimates we have attempted to utilize parameter values that understate inflows and overstate outflows. Our results are most sensitive to the assumptions we make about the probability of border apprehension and the voluntary emigration rates of undocumented immigrants leaving the United States. Further research could explore in greater detail the impact of assumptions about these parameters on estimates of the number of undocumented immigrants. To explore the uncertainty of our estimates we have conducted extension simulations over parameters, simulating 1 million different population trajectories; further research could widen the ranges of parameters and consider additional parameter uncertainty. Further research could also analyze inflows and outflows based on country of origin.

Our results lead us to the conclusion that the widely accepted estimate of 11.3 million undocumented immigrants in the United States is too small. Our model estimates indicate that the true number is likely to be larger, with an estimated ninety-five percent probability interval ranging from 16.2 to 29.5 million undocumented immigrants.

## Supporting information

S1 File. Supporting Material. Contains the mathematical model, parameter values, and data sources underlying the model. (PDF)

S2 File. Excel File. The spreadsheet used to calculate the conservative estimate.

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# The Number of Undocumented Immigrants in the United States: Estimates Based on Demographic 

Modeling with Data from 1990 to 2016
Supplementary Material

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Here we first explain the methods, parameter values and data sources we employ in producing our conservative estimate of 16.7 million undocumented immigrants. Then we describe the details of the simulation.

## 1 The Conservative Estimate

Let $N_{t}$ denote the number of undocumented immigrants at time $t$. In our model, we set the starting date to 1990 (i.e., $t=0$ corresponds to the beginning of

[^4]1990), assuming that $N_{0}=3,500,000$, a number in agreement with the standard estimate [1].

The number of undocumented immigrants at time $t$ is:

$$
\begin{equation*}
N_{t}=N_{t-1}+I_{t}-O_{t}, \quad t>0 \tag{S1}
\end{equation*}
$$

where $I_{t}$ and $O_{t}$ are the population inflows and outflows at time $t$, respectively (Table 1 summarizes notation).

Inflows: We decompose the population inflow, $I_{t}$, into (I) visa overstayers, $S_{t}$, and (II) illegal border crossers, $B_{t}$.
I. Visa Overstayers. Visa overstayers are non-immigrants who are admitted to the U.S. lawfully, but do not leave after the period during which they have been allowed to remain in the U.S. legally ends. DHS only started tracking visa overstayers from 2015 [2]. ${ }^{1}$ In our analysis, we focus on the 2016 visa overstayers since the 2015 number is incomplete (it only includes business and pleasure travelers). To get an estimate of the annual number of overstayers for 1990 onwards, we assume that it is proportional to the number of non-immigration visas issued by the state department, $V_{t}$, which is available for every year in our timespan [3]. ${ }^{2}$ Table 2 provides the number of visas issued for each year. Let

$$
\begin{equation*}
r=\frac{S_{27}}{V_{27}} \tag{S2}
\end{equation*}
$$

[^5]denote the ratio of visa overstayers to the number of individuals issued nonimmigration visas for 2016 ( $t=27$ corresponds to 2016). We use as our estimate of the visa overstayers for 1990 through 2015:
\[

$$
\begin{equation*}
S_{t}=r V_{t}, \quad t \geq 1 \tag{S3}
\end{equation*}
$$

\]

The assumption that the rate of overstays for all previous years is equal to the 2016 rate is in fact quite conservative. Let $\tau_{j}$ be the number of years a newly arriving undocumented immigrant in year $j$ remains in the country. Then $\operatorname{Pr}\left\{\tau_{j} \geq k\right\}$ is the probability that a new arrival in year $j$ is still present $k$ years later. The total number of visa overstayers present at year $t$ is

$$
\begin{equation*}
\sum_{j=1}^{t} S_{j} \operatorname{Pr}\left\{\tau_{j} \geq t-j\right\}=r \sum_{j=1}^{t} V_{j} \operatorname{Pr}\left\{\tau_{j} \geq t-j\right\} \tag{S4}
\end{equation*}
$$

Approximately $41 \%$ of undocumented immigrants based on the current survey data approach are visa overstayers [4], which translates to a visa overstay population of 4.6 million in 2015 . For formula $(S 4)$ to generate as many overstayers as the 4.6 million in the 11.3 million estimate, we would need to increase the visa overstay rate to $1.1 \times r$.
II. Illegal Border Crossers. We estimate the number of individuals who successfully cross the border in year $t, B_{t}$, using the data provided in the recent DHS report [5]. The report uses a repeated trials model [6], combined with data on apprehensions at the border, to estimate the rate of apprehension of individuals attempting to cross the Southern Border for each year from 2005 to the present (see Figure 1 for their results). In turn, these estimates
can be used to generate an estimate of $B_{t}$ for each year from 2005 to the present. Let $p_{t}$ be the probability (for year $t$ ) that an individual attempting to cross the border illegally is apprehended. Formula (S9) below is used by DHS to estimate $p_{t}$. Assume that an apprehended individual is returned to the original (foreign) side of the border, and that with probability $d_{t}$ the individual chooses not to try again; DHS provides estimates for $d_{t}$ for each year from 2005 to the present. Thus with probability $\left(1-d_{t}\right)$ an individual does not give up, and tries again to cross, again facing the probability $p_{t}$ of being apprehended. (We note that the deterrent effect of enforcement is implicitly controlled for, since this is one factor leading individuals to give up.) Let $C_{t}$ be the total number of individuals who wish to cross the border in year $t$ and will make at least one attempt. $C_{t} p_{t}$ individuals will be apprehended on their first attempt, and a fraction $\left(1-d_{t}\right)$ of these will attempt to cross again. It follows that $C_{t} p_{t}^{2}\left(1-d_{t}\right)$ individuals will attempt to cross a second time and be apprehended on their second attempt. Continuing in this way, a geometric series is generated that provides a formula for the total number of apprehensions that will be made, as well as the total number of repeat apprehensions, that is, apprehensions of individuals who tried to cross and were apprehended at least once earlier in the year. Let $A_{t}$ denote the total number of apprehensions (see Table 3), and $\bar{A}_{t}$ denote the number of repeat apprehensions. DHS [5] provides data for both of these. Applying the logic of the model:

$$
\begin{equation*}
A_{t}=C_{t} p_{t}+C_{t} p_{t}^{2}\left(1-d_{t}\right)+C_{t} p_{t}^{3}\left(1-d_{t}\right)^{2}+\ldots \tag{S5}
\end{equation*}
$$

$$
\begin{gather*}
A_{t}=C_{t} \frac{p_{t}}{1-p_{t}\left(1-d_{t}\right)},  \tag{S6}\\
\bar{A}_{t}=A_{t}-C_{t} p_{t} . \tag{S7}
\end{gather*}
$$

Thus,

$$
\begin{equation*}
\frac{\bar{A}_{t}}{A_{t}}=\frac{A_{t}-C_{t} p_{t}}{A_{t}}=1-\frac{C_{t} p_{t}}{C_{t} \frac{p_{t}}{1-p_{t}\left(1-d_{t}\right)}} . \tag{S8}
\end{equation*}
$$

It follows using algebra that

$$
\begin{equation*}
p_{t}=\frac{\bar{A}_{t} / A_{t}}{1-d_{t}} \tag{S9}
\end{equation*}
$$

Now let $Q_{t}$ denote the number of individuals who give up without having crossed successfully:

$$
\begin{equation*}
Q_{t}=C_{t} p_{t} d_{t}+C_{t} p_{t}^{2}\left(1-d_{t}\right) d_{t}+C_{t} p_{t}^{3}\left(1-d_{t}\right)^{2} d_{t}+\ldots=A_{t} d_{t} \tag{S10}
\end{equation*}
$$

Rearranging (S6):

$$
\begin{equation*}
C_{t}=A_{t} \frac{1-p_{t}\left(1-d_{t}\right)}{p_{t}} \tag{S11}
\end{equation*}
$$

The number of successful border crossers $B_{t}$ is equal to the difference between the initial pool of individuals who wish to cross, $C_{t}$, and the number who give up, $Q_{t}$ (all others eventually make it across successfully in this model). Thus

$$
\begin{equation*}
B_{t}=C_{t}-Q_{t}=A_{t} \frac{1-p_{t}\left(1-d_{t}\right)}{p_{t}}-A_{t} d_{t} \tag{S12}
\end{equation*}
$$

Finally,

$$
\begin{equation*}
B_{t}=A_{t} \frac{1-p_{t}}{p_{t}} \tag{S13}
\end{equation*}
$$

We make a few notes about this formula. First, the probability of apprehension is assumed to be constant across attempts. This rate could decrease, if individuals learn how to escape detection over time; and it could increase due to a selection effect with individuals better able to escape detection making it through after just one or a few trials. Second, the DHS estimates of the apprehension rates in [5] are subject to uncertainty. However, their estimates are larger than those elsewhere in the literature [7, 8], thus contributing to our overall conservative estimate (underestimate) of the number of border crossers. Third, we compared the above model with models where individuals quit if they fail $n$ times $(n>2)$. The results show that the number of border crossers in the repeated trial model is indeed lower than the crossers in these alternative models. Thus our model is again conservative in terms of the number of crossers we use in our analysis.

Most experts agree that the apprehension rate was significantly lower in earlier years and has been steadily increasing $[7,8]$. Another point of data in support of this is the fact that the number of border agents has increased dramatically over the timespan of our analysis [9] (see Table 4). Moreover, the number of hours spent by border agents patrolling the immediate border area increased by more than $300 \%$ between 1992-2004, and new infrastructure (e.g., fences) and technologies (e.g., night vision equipment, sensors, and video imaging systems) were introduced during this period [10]. Thus, for our conservative estimate we assume that the apprehension rate in years

1990-2004 was equal to the average rate in years $2005-10$ or $39 \%$; this is well above the rates discussed in the literature for earlier years and thus tends to reduce our estimate of the number of undocumented immigrants since it implies a larger fraction are apprehended at the border.

Outflows: The outflow $O_{t}$ is comprised of: (I) emigration, (II) mortality, (III) deportation, and (IV) adjustment of status from unauthorized to lawful.
I. Emigration. The emigration rate corresponds to the fraction of undocumented immigrants who leave the U.S. voluntarily. Since the propensity to emigrate decreases with the duration of stay [12], we consider durationdependent emigration rates; thus we employ separate emigration rates for those who have spent one year or less in the U.S., 2-10 years, or longer. We base our value for the 1-year emigration rate, $\mu_{s}$, on the 1-year visa overstay exit rate for 2016 ([11]; the rate for 2015 is similar), which is approximately $30 \%$ - this is the fraction of overstayers who left the country within one year from the day their visa expired. We again take a conservative stance by increasing the 1 -year rate to $40 \%$; thus among individuals who enter at time $t, 0.4 \times I_{t}$ will leave by time $t+1$. Note that this rate is especially an overestimate for illegal border crossers, who are widely viewed as having a lower likelihood of returning in the first year than visa overstayers [8]. For years 2-10, we draw on parameter values in the literature; these estimates fall from 0.01 to 0.04 [12-15]. For our conservative estimate calculation, we set the 2-10 year rate, $\mu_{m}$, equal to $4 \%$, the highest estimate in the literature. Published estimates of the emigration rate for individuals who have been in the country more than 10 years typically fall around $1 \%$, thus,
we equate this rate, $\mu_{l}$, to $1 \%$ per line with these estimates. Given that emigration rates depend upon time spent in the United States, the dynamic nature of our model results in different overall annual emigration rates for each year in our study, ranging from $5 \%$ to as high as $25 \%$. These rates are significantly higher than estimates of the emigration rate for those born outside the United States found in the literature or government sources; published estimates include $1 \%$ [14-17], 2.4\% [13], and 2.9\% [12]. The main reason the emigration rates in our model greatly exceed those found in the literature is the extremely high $40 \%$ emigration rate that we assume for those who have only been in the country for one year. To further enhance the conservatism of our model, we assume that all undocumented immigrants present at the beginning of 1990 have been here for only one year.
II. Mortality Rate. We set the mortality rate, $\delta$, equal to $0.7 \%$, the age-adjusted mortality rate reported by the Center for Disease Control and Prevention [18]. Note that this is generally viewed in the literature as an overestimate [13]. To further check that this rate is an overestimate, we combined the age, gender, and country of birth distributions of undocumented immigrants reported in [17, 19] with CDC mortality rates [18] (CDC reports death rates by age, race, and Hispanic origin). The resulting mortality rate is less than $0.2 \%$, much lower than the mortality rate we consider. Note that the mortality rate is quite small and does not have a large impact on our estimates.

III and IV. Deportations and Adjustments. The annual number of deportations and
adjustments (change from illegal to legal status), which we denote $D_{t}$, are taken directly from published data $[13,20,21]$. To overestimate the outflows, we include the deferred action for childhood arrivals (DACA) recipients in the annual adjustments [22]. Table 5 presents the annual number of deportations and adjustments in our timespan.

We use the following procedure to calculate our conservative estimate of the population of undocumented immigrants at each time $t$. Since the emigration rate depends on the duration of stay, we must keep track of entry times. If $t \leq 10$, calculating $N_{t}$ is straightforward - from equation (S1) we get:

$$
\begin{equation*}
N_{t}=N_{t-1}\left(1-\mu_{m}-\delta\right)+I_{t}\left(1-\mu_{s}\right)-D_{t} \quad t \leq 10 \tag{S14}
\end{equation*}
$$

If $t>10$, however, the formula becomes more complicated, as the exit rate of the population with age greater than 10 reduces to $\left(1-\mu_{l}-\delta\right)$. To incorporate this into equation (S1) let:

$$
\theta_{j}=\left\{\begin{array}{lr}
\left(1-\mu_{m}-\delta\right)^{10}\left(1-\mu_{l}-\delta\right)^{t-10}, & j=0 \\
\left(1-\mu_{m}-\delta\right)^{9}\left(1-\mu_{l}-\delta\right)^{t-j-9}, & 0<j \leq t-10 \\
\left(1-\mu_{m}-\delta\right)^{t-j}, & j>t-10
\end{array}\right.
$$

The number of undocumented immigrants at time $t>10$ is then:

$$
\begin{equation*}
N_{t}=N_{0} \theta_{0}+\sum_{j=1}^{t}\left(\left[I_{j}\left(1-\mu_{s}\right)-D_{j}\right] \theta_{j}\right), \quad t>10 \tag{S15}
\end{equation*}
$$

## 2 The Simulation

### 2.1 Methodology

Our simulation is designed to evaluate the range of outcomes the model produces, thus taking into account important sources of variability. There are two main sources of uncertainty, parameter uncertainty and the inherent variability of the population conditional upon parameter values. We take both sources into account.

We address parameter uncertainty by establishing ranges for key parameters. These key parameters are:
(i) the visa overstay rate, $r$;
(ii) border apprehension rates for individuals attempting to cross the border illegally, $p=\left\{p_{1}, \ldots, p_{27}\right\}$ (recall $t=27$ corresponds to the year 2016);
(iii) the voluntary emigration rate, which is set separately for illegal border crossers, $\mu_{s}^{\beta}$, and visa overstays for the first year, $\mu_{s}^{o}$; then jointly for both border crossers and visa overstays for years $2-10, \mu_{m}$; and jointly for years 10 and above, $\mu_{l}$. We also establish a cohort-specific range for each annual cohort from 1991-2016 for the first-year rate for illegal border crossers, $\mu_{s}^{\beta} \equiv\left\{\mu_{s, 1}^{b}, \ldots, \mu_{s, 27}^{b}\right\}$;
(iv) the mortality rate, $\delta$.

For each parameter we establish a uniform distribution over a set range (we will describe the parameter ranges in the next section).

To include the second source of variability, the inherently stochastic nature of the population, we impose a Poisson structure on our model. Specifically, conditional on all parameter values, which we represent by $\alpha \equiv\left\{r, p, \mu_{s}^{\beta}, \mu_{s}^{o}, \mu_{m}, \mu_{l}, \delta\right\}$, we model the overall population as the sum of Poisson variables, each of which
counts the number of people who enter at a given time and exit at a future time. Formally, let $\Lambda_{j, k}$ denote the number of arrivals at year $j$ who are still present $k$ years later, and $\operatorname{Pr}\left\{\tau_{j}^{i} \geq k\right\}, i \in\{o, b\}$ denote the probability that an individual undocumented immigrant in the cohort of type $i$ (overstayer or border crosser) arriving at year $j$ is still present $k$ years later. Then,

$$
\begin{equation*}
\Lambda_{j, k} \sim \operatorname{Poisson}\left(S_{j}(\alpha) \operatorname{Pr}\left\{\tau_{j}^{o}(\alpha) \geq k\right\}+B_{j}(\alpha) \operatorname{Pr}\left\{\tau_{j}^{b}(\alpha) \geq k\right\}\right),{ }^{3} \tag{S16}
\end{equation*}
$$

and the overall population is

$$
\begin{equation*}
N_{t}=\sum_{j=0}^{t} \Lambda_{j, t-j} . \tag{S17}
\end{equation*}
$$

We assume that the Poisson variables $S_{j}(\alpha)$ and $B_{j}(\alpha)$ are mutually independent conditional on the parameters $\alpha$ for all time periods $j$, and also that $S_{j}(\alpha)\left(B_{j}(\alpha)\right)$ is independent of $\tau_{j}^{o}(\alpha)\left(\tau_{j}^{b}(\alpha)\right)$ for all $j$, again conditional on the parameters. The first assumption means that given the parameter values, the number of visa overstayers in any given year does not depend upon the number of border crossers in any other year. This is a reasonable assumption as possible correlations that might arise among these two arrival types are already captured in the parameters. The second assumption simply means that the duration an arriving individual remains in the country does depend upon the year of arrival, but does not depend upon the number of arrivals. Since the sum of independent Poisson variables is also Poisson, the population size $N_{t}$ conditional on the parameters $\alpha$ is also

[^6]Poisson distributed, that is:
$N_{t}(\alpha) \sim$ Poisson $\left(\sum_{j=0}^{t}\left(S_{j}(\alpha) \operatorname{Pr}\left\{\tau_{j}^{o}(\alpha) \geq t-j\right\}+B_{j}(\alpha) \operatorname{Pr}\left\{\tau_{j}^{b}(\alpha) \geq t-j\right\}\right)\right)$.

Thus, each simulation run follows two steps: (i) a random draw of the parameter vector, which we denote by $\widetilde{\alpha}$, and a draw for the initial population of undocumented immigrants in 1990 , denoted by $n_{0}$; and (ii) conditional upon $\widetilde{\alpha}$, a draw for the population at year $t, n_{t}(\widetilde{\alpha})$, for $t=1,2, \ldots, 27$.

### 2.2 Parameter Ranges

The parameters are uniformly drawn from the following ranges:

1. Visa overstay rate: for each simulation, the visa overstay rate is set equal to the 2016 rate multiplied by a uniform draw from the range [.5,1.5].
2. Probability of apprehension:
(a) 1990 to 2004: for these earlier years we assume a uniform distribution over the range [.25,.40].
(b) 2005 to 2015: for each year between 2005 to 2010, we use the numbers in [8] as lower bounds, the DHS numbers in [5] as the mid-points, and the DHS numbers in [5] plus the difference between the DHS numbers and the numbers in [8] as upper bounds. The apprehension probabilities are then selected at random between these lower and upper bounds. Since [8] only provides the probability of apprehension up to 2010, for 2011 to 2015, we use five year rolling averages to get the lower and upper bounds.
3. Voluntary emigration:
(a) First-year rates:
i. For visa overstayers we assume the first-year rate falls in the range [.25,.50] for each year.
ii. For illegal border crossers, there are data indicating that first-year rates vary across cohorts [8]. To incorporate this, we assume that a voluntary emigration rate is drawn for each cohort year from a uniform distribution that is specific to that cohort's year of initial entry; the lower bound of this range is set by the numbers in [8] and the upper bound is set at 0.50 .
(b) For years 2-10 we assume a range [.01,.05].
(c) For years 10 and above we draw a value from the range [.005,.02].
4. Mortality: this rate is drawn from the range [.005,.01].
5. To capture circular flows, we impose a negative correlation between the first-year emigration rate and the border apprehension rate for illegal border crossers; based on our own analysis for annual data from the best recent study [8] we use a correlation of -0.5. Specifically, we generate two correlated random variables, one for the probability of apprehension and the other for the first-year emigration rate of border crossers from the ranges described above.

## Figures and Tables



Figure 1: Southern Border Apprehension Rate 2005-2015 - Data Source: U.S. Department of Homeland Security [4]

Table 1. Notation

| Parameter | Description |
| :---: | :--- |
| $N_{t}$ | Number of undocumented immigrants at time $t$ |
| $S_{t}$ | Number of visa overstays at time $t$ |
| $B_{t}$ | Number of border crossers at time $t$ |
| $I_{t}$ | Total inflow at time $t$ |
| $V_{t}$ | Number of non-immigration visas at time $t$ |
| $C_{t}$ | Number of individuals wishing to cross the border at time $t$ |
| $Q_{t}$ | Number of individuals who give up without having to cross at time $t$ |
| $r$ | Overstay rate |
| $p_{t}$ | Border apprehension rate at time $t$ |
| $d_{t}$ | Probability of giving up at time $t$ |
| $A_{t}$ | Number of border apprehensions at time $t$ |
| $\bar{A}_{t}$ | Number of repeat apprehensions at time $t$ |
| $\mu_{s}$ | First year emigration rate |
| $\mu_{m}$ | 2-10 year emigration rate <br> $\mu_{l}$ |
| More than 10 year emigration rate <br> $D_{t}$ | Number of deportations and adjustments at time $t$ <br> $\delta$ |
| Age-adjusted average mortality rate |  |
| $\Lambda_{j, k}$ | number of arrivals at year $j$ who are still present $k$ years later |
| $\left.O_{t} \geq k\right\}$ | Probability that a new arrival in year $j$ is still present $k$ years later |
| $\tau_{j}$ |  |

Table 2. Number of Non-Immigration Visa Issues

| Year | Visas | Year | Visas |
| :---: | :---: | :---: | :---: |
| 1990 | $4,850,670$ | 2004 | $3,821,822$ |
| 1991 | $5,026,298$ | 2005 | $4,174,816$ |
| 1992 | $4,576,644$ | 2006 | $4,722,102$ |
| 1993 | $4,418,952$ | 2007 | $5,188,127$ |
| 1994 | $4,551,906$ | 2008 | $5,398,167$ |
| 1995 | $5,106,963$ | 2009 | $4,661,000$ |
| 1996 | $5,333,575$ | 2010 | $5,026,509$ |
| 1997 | $5,162,948$ | 2011 | $5,910,719$ |
| 1998 | $5,148,774$ | 2012 | $6,958,609$ |
| 1999 | $5,164,066$ | 2013 | $7,416,050$ |
| 2000 | $5,268,821$ | 2014 | $8,220,061$ |
| 2001 | $5,241,895$ | 2015 | $9,189,856$ |
| 2002 | $4,003,965$ | 2016 | $8,755,614$ |
| 2003 | $3,642,277$ |  |  |

Source: U.S. Department of State [3]

Table 3. Apprehensions on the Southern Border

| Year | Apprehensions | Year | Apprehensions |
| :---: | :---: | :---: | :---: |
| 1990 | $1,049,321$ | 2004 | $1,139,282$ |
| 1991 | $1,077,876$ | 2005 | $1,171,396$ |
| 1992 | $1,145,574$ | 2006 | $1,071,972$ |
| 1993 | $1,212,886$ | 2007 | 858,638 |
| 1994 | 979,101 | 2008 | 705,005 |
| 1995 | $1,271,390$ | 2009 | 540,865 |
| 1996 | $1,507,020$ | 2010 | 447,731 |
| 1997 | $1,368,707$ | 2011 | 327,577 |
| 1998 | $1,516,680$ | 2012 | 356,873 |
| 1999 | $1,537,000$ | 2013 | 414,397 |
| 2000 | $1,643,679$ | 2014 | 479,371 |
| 2001 | $1,235,718$ | 2015 | 331,333 |
| 2002 | 929,809 | 2016 | 408,000 |
| 2003 | 905,065 |  |  |

Source: U.S. Department of Homeland Security [21]

Table 4. Number of Border Agents

| Year | Border Agents | Year | Border Agents |
| :---: | :---: | :---: | :---: |
| 1992 | 3,555 | 2005 | 9,891 |
| 1993 | 3,444 | 2006 | 11,032 |
| 1994 | 3,747 | 2007 | 13,297 |
| 1995 | 4,388 | 2008 | 15,442 |
| 1996 | 5,333 | 2009 | 17,408 |
| 1997 | 6,315 | 2010 | 17,535 |
| 1998 | 7,357 | 2011 | 18,506 |
| 1999 | 7,706 | 2012 | 18,546 |
| 2000 | 8,580 | 2013 | 18,611 |
| 2001 | 9,147 | 2014 | 18,156 |
| 2002 | 9,239 | 2015 | 17,522 |
| 2003 | 9,840 | 2016 | 17,206 |
| 2004 | 9,506 |  |  |

Source: U.S. Customs and Border Protection [9]

Table 5. Annual Number of Deportations and Adjustments

| Year | Deportations | Adjustments | Year | Deportations | Adjustments |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1990 | 25,369 | 37,883 | 2004 | 107,313 | 84,288 |
| 1991 | 28,568 | 35,290 | 2005 | 108,056 | 79,037 |
| 1992 | 33,921 | 42,925 | 2006 | 113,576 | 64,200 |
| 1993 | 34,023 | 44,870 | 2007 | 175,344 | 94,064 |
| 1994 | 34,921 | 38,392 | 2008 | 150,078 | 100,485 |
| 1995 | 35,765 | 41,900 | 2009 | 164,839 | 104,029 |
| 1996 | 41,426 | 55,428 | 2010 | 185,128 | 88,363 |
| 1997 | 58,954 | 54,319 | 2011 | 181,555 | 90,228 |
| 1998 | 64,797 | 61,448 | 2012 | 148,153 | 247,864 |
| 1999 | 65,287 | 60,393 | 2013 | 110,094 | 523,323 |
| 2000 | 65,279 | 72,621 | 2014 | 102,224 | 181,220 |
| 2001 | 71,191 | 176,169 | 2015 | 69,478 | 114,115 |
| 2002 | 80,836 | 114,927 | 2016 | 65,332 | 167,165 |
| 2003 | 101,750 | 119,709 |  |  |  |

Source: U.S. Department of Homeland Security [13, 20, 21, 22]

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[^0]:    ${ }^{1}$ Our model as well as most work in the literature indicates that the population size has been relatively stable since 2008; thus 2015 and 2016 are quite comparable.
    ${ }^{2}$ The estimate of 3.5 million undocumented immigrants in 1990 is based on applying the residual method (using the 1980 and 1990 censuses), described previously, which we argue systematically underestimates the population. Thus in assuming an initial population of 3.5 million, and centering our simulations around this value, we are almost certainly underestimating the size of the undocumented immigrant population at this date.

[^1]:    ${ }^{3}$ That is, in our model most undocumented immigrants are not overstayers, and the model produces an estimate of the number of overstayers below the estimate produced in the conventional approach based on survey data.
    ${ }^{4}$ Since many overstayers leave or adjust their status within a few months of their visa expiration date, we make a further conservative adjustment and count as overstayers only those individuals who have overstayed more than 1 year.

[^2]:    ${ }^{5}$ However, we note that these additional border resources may have been concentrated in certain locations and it remains a possibility that apprehension rates were higher in earlier years.
    ${ }^{6}$ We note that reference (12) estimates that the probability of eventual entry after multiple attempts on a single trip in the 1990s is close to one, indicating almost no deterrence in the earlier period.

[^3]:    ${ }^{7}$ This is based on analyzing our model using the conservative estimate values for all other parameters.
    8 The rate for 2015 is similar.
    9 To further enhance the conservatism of our model, we assume that all undocumented immigrants present at the beginning of 1990 have been here for only one year.

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[^5]:    ${ }^{1}$ The visa overstay number only includes arrivals via air and sea.
    ${ }^{2}$ See [2] for the list of non-immigration visa types that can potentially lead to a visa overstay.

[^6]:    ${ }^{3}$ Given that we only have yearly deportation and adjustment of status data, we adjust $\Lambda_{j, k}$ by correcting for $D_{j}$.

